

• $3x$ (") $x -$.
 • (") B A $s -$
 " 14 ,

• $\frac{1}{3}$, 20 -

• , ,
 :

$s -$ "	$v -$ "	$t -$	
14	x	$\frac{14}{x}$	C - " 14 - C
14	$3x$	$\frac{14}{3x}$	C - " 14 - C
$6x$	$3x$	2	C - A -
$s - 6x$	x	$\frac{s - 6x}{x}$	B - C -
s	$3x$	$\frac{s}{3x}$	B - A -

• $\frac{14}{x} = \frac{14}{3x} + \frac{1}{3}$: , ,

• $\frac{2}{3}$, 40 -

• $\frac{2}{3} + \frac{s}{3x} = 2 + \frac{s - 6x}{x}$: , ,

"

:

$$\begin{cases} \frac{14}{x} = \frac{14}{3x} + \frac{1}{3} \\ \frac{2}{3} + \frac{s}{3x} = 2 + \frac{s-6x}{x} \end{cases}$$

$$1. \frac{14}{x} = \frac{14}{3x} + \frac{1}{3}$$

$$\frac{28}{3x} = \frac{1}{3}$$

$$\boxed{x=28}$$

$$2. \frac{2}{3} + \frac{s}{3 \cdot 28} = 2 + \frac{s-6 \cdot 28}{28}$$

$$\frac{s}{84} = \frac{4}{3} + \frac{s-168}{28}$$

$$\frac{s}{84} = \frac{4}{3} + \frac{s}{28} - \frac{168}{28}$$

$$-\frac{s}{42} = -\frac{14}{3}$$

$$\boxed{s=196}$$

, " $28 \cdot 3 = 84$, " 196

B A

$$\cdot \frac{196}{84} = 2\frac{1}{3}$$

.() $2\frac{1}{3}$

B A , :

. " 84 :

.1, -5, 9, -13, 17, -21, ...

$$. -4 \quad (\quad + \quad)$$

$$a_n + a_{n+1} = a_n + (-a_n - 4)$$

$$a_n + a_{n+1} = a_n - a_n - 4$$

$$a_n + a_{n+1} = -4$$

$$. -4n \quad \quad \quad 2n \quad ,$$

$$. S_{2n-1} = 101$$

$$. -8 \quad \quad -5$$

$$a_{2n} = -5 - 8(n-1)$$

$$. a_{2n} = -5 - 8n + 8$$

$$a_{2n} = -8n + 3$$

$$. -4n - (-8n + 3) = 101 :$$

$$-4n + 8n - 3 = 101$$

$$. 4n = 104 \quad / : 4$$

$$n = 26$$

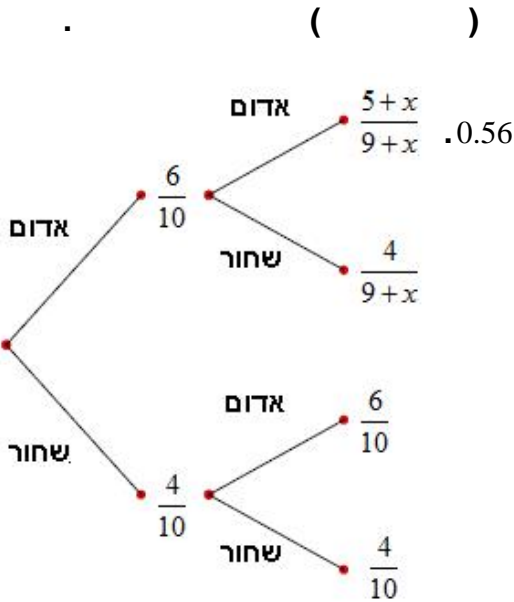
$$. 8 \quad \quad 1 \quad \quad -$$

$$S_{26} = \frac{26(2 \cdot 1 + 8(26-1))}{2}$$

$$S_{26} = 13(2 + 200)$$

$$\boxed{S_{26} = 2,626}$$

$$. 2,626 \quad \quad - \quad \quad n(= 26) \quad :$$



$$0.56 = \frac{4}{10} \cdot \frac{4}{10} + \frac{6}{10} \cdot \frac{5+x}{9+x}$$

$$0.56 = 0.16 + 0.6 \cdot \frac{5+x}{9+x} \quad / -0.16$$

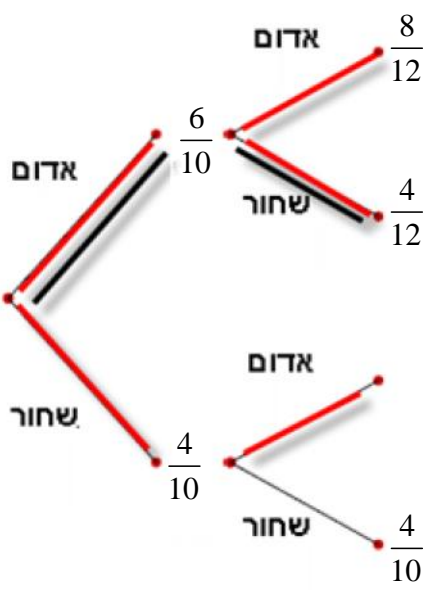
$$0.4 = 0.6 \cdot \frac{5+x}{9+x} \quad / : 0.6$$

$$\frac{2}{3} = \frac{5+x}{9+x} \quad / \cdot 3(9+x)$$

$$2(9+x) = 3(5+x)$$

$$18 + 2x = 15 + 3x$$

$$\boxed{x=3}$$



$x=3$:

$$p(\text{the 2nd ball is black} / \text{at least one ball is red}) =$$

$$= \frac{P(\text{the 2nd ball is black} \cap \text{at least one ball is red})}{P(\text{at least one ball is red})} =$$

$$= \frac{\frac{6}{10} \cdot \frac{4}{12}}{1 - \frac{4}{10} \cdot \frac{4}{10}} = \frac{0.2}{1 - 0.16} = \frac{5}{21}$$

$\frac{5}{21}$:

$$k=1, p = \frac{6}{10} \cdot \frac{8}{12} = 0.4, n = n$$

:

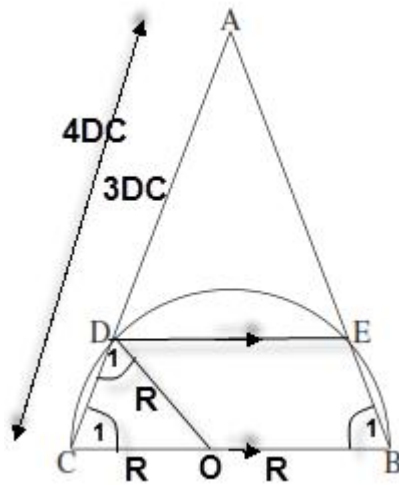
$$P_n(1) = \binom{n}{1} \cdot (0.4)^1 \cdot (1-0.4)^{n-1}$$

$$P_n(1) = \frac{n!}{1!(n-1)!} \cdot 0.4 \cdot 0.6^{n-1}$$

$$P_n(1) = \frac{(n-1)! \cdot n}{1(n-1)!} \cdot 0.4 \cdot \frac{0.6^n}{0.6}$$

$$P_n(1) = \frac{2}{3} n \cdot 0.6^n$$

$$\frac{2}{3} n \cdot 0.6^n :$$



(AB = AC)

ΔABC .1

BC .2

.R

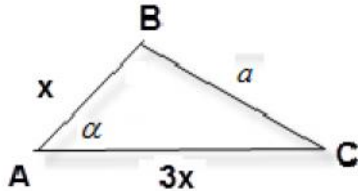
.4 $DC = \frac{1}{3}AD$.3 :

BCDE . : "

$R = \sqrt{2}DC$.

	AB = AC	5	1
,	$AD \cdot AC = AE \cdot AB$	6	
	AD = AE	7	6,5
	DC = EB	8	7,5
	$\frac{AD}{DC} = \frac{AE}{EB}$	9	8,7
	DE CB	10	9
A	$CD \not\parallel EB$	11	
	BCDE	12	11,10
	BCDE	13	12,8
. . .			
	BC = 2R	14	4,2
	OD = OC = OB = R	15	14,4
ΔODC	$\sphericalangle C_1 = \sphericalangle D_1$	16	15
ΔABC	$\sphericalangle C_1 = \sphericalangle B_1$	17	5
	$\sphericalangle C_1 = \sphericalangle C_1, \sphericalangle D_1 = \sphericalangle B_1$	18	17,16
	$\Delta ODC \sim \Delta ABC$	19	18

	$\frac{OD}{AB} = \frac{OC}{AC} = \frac{DC}{BC}$	20	19
	$DC = \frac{1}{3}AD$	21	3
	$AC = 4DC$	22	21
	$\frac{R}{4DC} = \frac{DC}{2R}$	23	22 ,20 ,15 ,14
	$R^2 = 2DC$	24	23
	$R = \sqrt{2}DC$	25	24
. . .			



$$\frac{AB}{AC} = \frac{1}{3} \cdot \quad .$$

$$(\quad) AB = x$$

$$(\quad) AC = 3x$$

$$(\quad) BC = a$$

$$(\quad) \sphericalangle A = \gamma$$

ΔABC

$$(BC)^2 = (AB)^2 + (AC)^2 - 2AB \cdot AC \cdot \cos \sphericalangle A$$

$$a^2 = x^2 + (3x)^2 - 2 \cdot x \cdot 3x \cdot \cos \gamma$$

$$a^2 = x^2 + 9x^2 - 6x^2 \cos \gamma$$

$$a^2 = x^2(10 - 6\cos \gamma)$$

$$x^2 = \frac{a^2}{10 - 6\cos \gamma}$$

$$S_{\Delta ABC} = \frac{1}{2} AB \cdot AC \cdot \sin \sphericalangle BAC$$

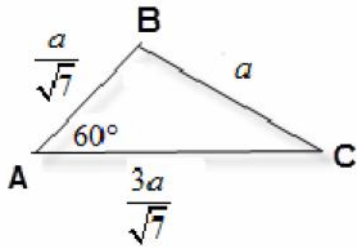
$$S_{\Delta ABC} = \frac{1}{2} \cdot x \cdot 3x \cdot \sin \gamma$$

$$S_{\Delta ABC} = \frac{3}{2} \cdot x^2 \cdot \sin \gamma$$

$$S_{\Delta ABC} = \frac{3}{2} \cdot \frac{a^2}{10 - 6\cos \gamma} \cdot \sin \gamma$$

$$S_{\Delta ABC} = \frac{3a^2 \sin \gamma}{20 - 12\cos \gamma}$$

$$S_{\Delta ABC} = \frac{3a^2 \sin \gamma}{20 - 12\cos \gamma} :$$



$$\angle A = 60^\circ$$

$$x^2 = \frac{a^2}{10 - 6\cos 60^\circ}$$

$$x^2 = \frac{a^2}{7} \quad / \sqrt{\quad}$$

$$\boxed{x = \frac{a}{\sqrt{7}}} \quad \leftarrow x > 0$$

$\triangle ABC$

$$AB = \frac{a}{\sqrt{7}}$$

$$BC = a$$

$$\frac{AB}{\sin \angle C} = \frac{BC}{\sin \angle A}$$

$$\frac{a}{\sqrt{7} \sin \angle C} = \frac{a}{\sin 60^\circ}$$

$$\frac{\cancel{a} \sin 60^\circ}{\cancel{a} \sqrt{7}} = \sin \angle C$$

$$\boxed{\angle C = 19.11^\circ} \quad \cancel{\angle C = 160.89^\circ}$$

$$180^\circ$$

$$\angle B = 180^\circ - 19.11^\circ - 60^\circ$$

$$\boxed{\angle B = 100.89^\circ}$$

$\triangle ABC$

$$\cos \angle C = \frac{(BC)^2 + (AC)^2 - (AB)^2}{2BC \cdot AC}$$

$$\cos \angle C = \frac{a^2 + \left(\frac{3a}{\sqrt{7}}\right)^2 - \left(\frac{a}{\sqrt{7}}\right)^2}{2a \cdot \frac{3a}{\sqrt{7}}}$$

$$\cos \angle C = \frac{\frac{15}{7}a^2}{\frac{6}{\sqrt{7}}a^2}$$

$$\boxed{\angle C = 19.11^\circ}$$

$$\angle B = 100.89^\circ, \quad \angle C = 19.11^\circ$$

$$0 \leq x \leq f \quad \boxed{f(x) = 2x + 8\cos^2\left(\frac{x}{2}\right) - \sin(2x)} :$$

$$f'(x) = 4\sin^2 x - 4\sin x \quad (1)$$

$$f'(x) = 2 + 8 \cdot 2\cos\left(\frac{x}{2}\right) \cdot \left(-\sin\left(\frac{x}{2}\right)\right) \cdot \left(\frac{1}{2}\right) - 2\cos(2x)$$

$$f'(x) = 2 - 8\sin\left(\frac{x}{2}\right)\cos\left(\frac{x}{2}\right) - 2(1 - 2\sin^2 x)$$

$$f'(x) = 2 - 4\sin x - 2 + 4\sin^2 x$$

$$\boxed{f'(x) = 4\sin^2 x - 4\sin x}$$

$$f'(x) \quad (2)$$

$$f'(x) \quad (2)$$

$$f'(0) = 4\sin^2 0 - 4\sin 0 \rightarrow \boxed{(0,0)}$$

$$f'(f) = 4\sin^2 f - 4\sin f \rightarrow \boxed{(f,0)}$$

$$\boxed{f''(x) = 8\sin x \cos x - 4\cos x}$$

$$0 = 4\cos x(2\sin x - 1)$$

$$\cos x = 0 \quad \sin x = 0.5$$

$$x = \frac{f}{2} + f k \quad x = \frac{f}{6} + 2f k \quad x = \frac{5f}{6} + 2f k$$

$$x = \frac{f}{2} \rightarrow f'\left(\frac{f}{2}\right) = 4\sin^2 \frac{f}{2} - 4\sin \frac{f}{2} \rightarrow \boxed{\left(\frac{f}{2}, 0\right)}$$

$$x = \frac{f}{6} \rightarrow f'\left(\frac{f}{6}\right) = 4\sin^2 \frac{f}{6} - 4\sin \frac{f}{6} \rightarrow \boxed{\left(\frac{f}{6}, -1\right)}$$

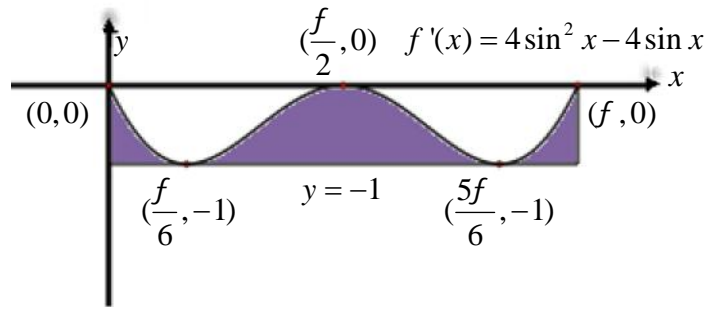
$$x = \frac{5f}{6} \rightarrow f'\left(\frac{5f}{6}\right) = 4\sin^2 \frac{5f}{6} - 4\sin \frac{5f}{6} \rightarrow \boxed{\left(\frac{5f}{6}, -1\right)}$$

0		$\frac{f}{6}$		$\frac{f}{2}$		$\frac{5f}{6}$		f	x
0		-1		0		-1		0	f'(x)
		0		0		0			f''(x)
Max	↘	Min	↗	Max	↘	Min	↗	Max	

$$\left(\frac{5f}{6}, -1\right), \left(\frac{f}{6}, -1\right), (f, 0), \left(\frac{f}{2}, 0\right), (0, 0) :$$

, $f'(x)$

(1)



(2)

(2)

$$-1 \leq f'(x) = 4 \sin^2 x - 4 \sin x \leq 0 \quad 0 \leq x \leq f$$

$$-0.25 \leq \sin^2 x - \sin x \leq 0 : \quad 4 -$$

$$\sin^2 x - \sin x = k$$

$$-0.25 \leq k \leq 0$$

$$-0.25 \leq k \leq 0 :$$

.()

$$S = \int_0^f (f'(x) - (-1)) dx =$$

$$S = \int_0^f (f'(x) + 1) dx =$$

$$S = \left[f(x) + x \right]_0^f =$$

$$S = (f(f) + f) - (f(0) + 0)$$

$$f(f) = 2f + 8 \cos^2(f) - \sin(2f) = 2f$$

$$f(0) = 2 \cdot 0 + 8 \cos^2(0) - \sin(2 \cdot 0) = 8$$

$$S = (2f + f) - (8 + 0)$$

$$\boxed{S = 3f - 8}$$

$$. 3f - 8$$

:

$$f(x) = \frac{x}{\sqrt{x^2 - 15}}$$

0 - - , (1)

$$x = \pm\sqrt{15} \quad , x^2 - 15 > 0$$

$$. x < -\sqrt{15} \quad x > \sqrt{15} : \quad :$$

(! . ,)

$$f(x) = \frac{x}{\sqrt{x^2 - 15}} = \frac{x}{|x|\sqrt{1 - \frac{15}{x^2}}}$$

$$\lim_{x \rightarrow +\infty} \frac{x}{|x|\sqrt{1 - \frac{15}{x^2}}} = \lim_{x \rightarrow +\infty} \frac{x}{x\sqrt{1 - \frac{15}{x^2}}} = 1 \rightarrow \boxed{y=1} \quad \lim_{x \rightarrow -\infty} \frac{x}{|x|\sqrt{1 - \frac{15}{x^2}}} = \lim_{x \rightarrow -\infty} \frac{x}{-x\sqrt{1 - \frac{15}{x^2}}} = -1 \rightarrow \boxed{y=-1}$$

$$\lim_{x \rightarrow \sqrt{15}^+} \frac{x}{\sqrt{x^2 - 15}} = \lim_{x \rightarrow \sqrt{15}^+} \frac{\sqrt{15}}{0^+} = +\infty \rightarrow \boxed{x = \sqrt{15}} \quad \lim_{x \rightarrow -\sqrt{15}^-} \frac{x}{\sqrt{x^2 - 15}} = \lim_{x \rightarrow -\sqrt{15}^-} \frac{-\sqrt{15}}{0^+} = -\infty \rightarrow \boxed{x = -\sqrt{15}}$$

$$, (x \rightarrow -\infty)y = -1, (x \rightarrow +\infty)y = 1 : x - \quad :$$

$$x = -\sqrt{15} , x = \sqrt{15} : y -$$

(3)

$$f'(x) = \frac{\sqrt{x^2 - 15} - \cancel{x} \cdot x}{(\sqrt{x^2 - 15})^2} = \frac{x^2 - 15 - x^2}{(x^2 - 15)^2}$$

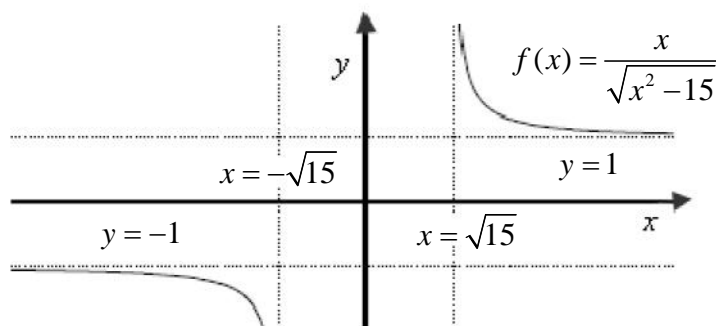
$$\boxed{f'(x) = \frac{-15}{(x^2 - 15)\sqrt{x^2 - 15}}}$$

.()

$$x < -\sqrt{15} \quad x > \sqrt{15}$$

$$. x : \quad , x < -\sqrt{15} \quad x > \sqrt{15} : \quad :$$

: (4)



$$g(x) = \frac{\sqrt{x^2 - 15}}{x}$$

$$x \leq -\sqrt{15} \quad x \geq \sqrt{15}$$

$$x = 0$$

$$x \leq -\sqrt{15} \quad x \geq \sqrt{15}$$

y -

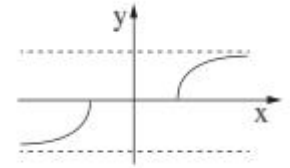
$$f(x) = -$$

$$g(x) = \frac{1}{f(x)}$$

$$g'(x) = \frac{-f'(x)}{f^2(x)}$$

$$g(x)$$

II



II

$$\frac{f'(x)}{g'(x)} < 0$$

x

$$x < -\sqrt{15} \quad x > \sqrt{15}$$

$$f'(x) < 0$$

$$g'(x) > 0$$

$$x < -\sqrt{15} \quad x > \sqrt{15}$$

$$g(x)$$

$$x < -\sqrt{15} \quad x > \sqrt{15} :$$

מינימום גובה ה-BCO.

$B(t, t^2 - 12)$, $y = x^2 - 12$, B

$0 < t < \sqrt{12}$

ΔBCO , $BC = BO$

OC , x - C

BD

$BD = y_D - y_B = 0 - (t^2 - 12) = 12 - t^2$, y - BD

$OC = 2t$ $OD = x_D - x_O = t - 0 = t$

$$S(t) = \frac{2t(12 - t^2)}{2}$$

$$S(t) = 12t - t^3$$

$$S'(t) = 12 - 3t^2$$

$$0 = 12 - 3t^2$$

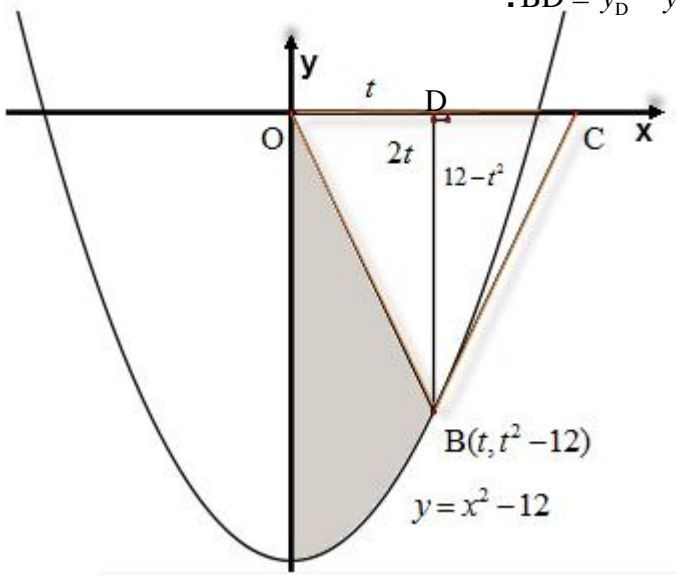
$$3t^2 = 12 \quad /:3$$

$$t^2 = 4 \quad / \sqrt{\quad}$$

$$t = 2 \quad 0 < t < \sqrt{12}$$

$$S''(t) = -6t$$

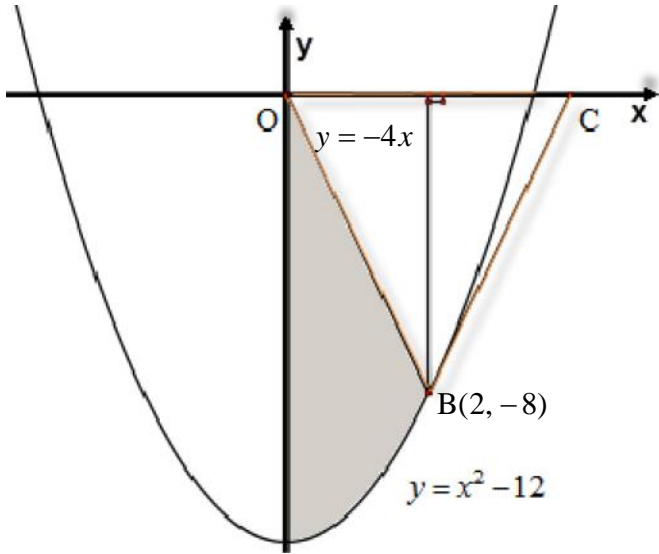
$$S''(2) = -12 < 0 \rightarrow \text{Max}$$



$(2, -8)$

BCO

B



.OB

$$m_{OB} = \frac{-8-0}{2-0} = -4$$

. $y = -4x$, ,OB

$$S = \int_0^2 (-4x - (x^2 - 12)) dx$$

$$S = \int_0^2 (-4x - x^2 + 12) dx$$

$$S = \left[\frac{-4x^2}{2} - \frac{x^3}{3} + 12x \right]_0^2$$

$$S = (-2 \cdot 2^2 - \frac{2^3}{3} + 12 \cdot 2) - (-2 \cdot 0^2 - \frac{0^3}{3} + 12 \cdot 0)$$

$$\boxed{S = 13\frac{1}{3}}$$

. $13\frac{1}{3}$: