

. (, ")

x -

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| s - " | v - " | t - | |
|---|----------|---------------------------------|---|
| $\frac{3}{4}x$ | x | $\frac{3}{4}$ | A |
| 10 | 50 | $\frac{1}{5}$ | |
| - | - | $\frac{33}{60} = \frac{11}{20}$ | |
| $120 - (\frac{3}{4}x - 10) = 130 - \frac{3}{4}x = \frac{520 - 3x}{4}$ | $x - 10$ | $\frac{520 - 3x}{4(x - 10)}$ | B |

$$\frac{120}{x}, \text{ " } 120 \quad x, \text{ ,}$$

, B -

$$\frac{3}{4} + \frac{1}{5} + \frac{11}{20} + \frac{520 - 3x}{4(x - 10)} = \frac{120}{x} + 1 :$$

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$$\frac{3}{4} + \frac{1}{5} + \frac{11}{20} + \frac{520 - 3x}{4(x - 10)} = \frac{120}{x} + 1$$

$$\frac{1}{2} + \frac{520 - 3x}{4(x - 10)} = \frac{120}{x} \quad / \cdot 4x(x - 10)$$

$$2x(x - 10) + x(520 - 3x) = 480(x - 10)$$

$$2x^2 - 20x + 520x - 3x^2 = 480x - 4800$$

$$-x^2 + 20x + 4800 = x$$

$$x_{1,2} = \frac{-20 \pm 140}{-2}$$

$$\boxed{x = 80} \quad \leftarrow x > 0$$

. " 80

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$$n=1 \quad .1 .$$

$$2 \cdot 4 + 5 \cdot 4^2 = 88 \quad ; \quad \frac{(6 \cdot 1 - 2) \cdot 4^{2 \cdot 1 + 1} + 8}{3} = \frac{264}{3} = 88 \quad ;$$

$$n=1$$

$$, (\quad) \quad n=k \quad .2$$

$$2 \cdot 4 + 5 \cdot 4^2 + 8 \cdot 4^3 + 11 \cdot 4^4 + \dots + (6k-1) \cdot 4^{2k} = \frac{(6k-2) \cdot 4^{2k+1} + 8}{3} \quad ;$$

$$" \quad , n=k+1 \quad .3$$

$$\frac{2 \cdot 4 + 5 \cdot 4^2 + 8 \cdot 4^3 + 11 \cdot 4^4 + \dots + (6k-1) \cdot 4^{2k} + (6k+2) \cdot 4^{2k+1} + (6k+5) \cdot 4^{2k+2}}{3} = \frac{(6k+4) \cdot 4^{2k+3} + 8}{3}$$

$$\downarrow$$

$$\frac{(6k-2) \cdot 4^{2k+1} + 8}{3} + (6k+2) \cdot 4^{2k+1} + (6k+5) \cdot 4^{2k+2} = \frac{(6k+4) \cdot 4^{2k+3} + 8}{3}$$

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$$\Leftrightarrow \frac{(6k-2) \cdot 4^{2k+1} + 8 + 3(6k+2) \cdot 4^{2k+1} + 3(6k+5) \cdot 4^{2k+2}}{3} = \frac{(6k+4) \cdot 4^{2k+3} + 8}{3}$$

$$\Leftrightarrow \frac{(6k-2) \cdot 4^{2k+1} + 3(6k+2) \cdot 4^{2k+1} + 12(6k+5) \cdot 4^{2k+1} + 8}{3} = \frac{16(6k+4) \cdot 4^{2k+1} + 8}{3}$$

$$\Leftrightarrow \frac{4^{2k+1}(6k-2+3(6k+2)+12(6k+5))+8}{3} = \frac{16(6k+4) \cdot 4^{2k+1} + 8}{3}$$

$$\Leftrightarrow \frac{4^{2k+1}(6k-2+18k+6+72k+60)+8}{3} = \frac{16(6k+4) \cdot 4^{2k+1} + 8}{3}$$

$$\Leftrightarrow \frac{4^{2k+1}(96k+64)+8}{3} = \frac{16(6k+4) \cdot 4^{2k+1} + 8}{3}$$

$$\Leftrightarrow \frac{4^{2k+1} \cdot 16(6k+4) + 8}{3} = \frac{16(6k+4) \cdot 4^{2k+1} + 8}{3}$$

$$, n=1 \quad .4$$

$$, n=k$$

$$n=k+1$$

. n , - ,

$$2 \cdot 4 + 5 \cdot 16 + 8 \cdot 64 \dots + 26 \cdot 262,144$$

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$$n = 4$$

$$2 \cdot 4 + 5 \cdot 4^2 + 8 \cdot 4^3 + 11 \cdot 4^4 + \dots + (6 \cdot 4 - 1) \cdot 4^{2^4} = \frac{(6 \cdot 4 - 2) \cdot 4^{2^4+1} + 8}{3}$$

$$2 \cdot 4 + 5 \cdot 4^2 + 8 \cdot 4^3 + 11 \cdot 4^4 + \dots + 23 \cdot 4^8 = 1,922,392$$

$$2 \cdot 4 + 5 \cdot 4^2 + 8 \cdot 4^3 + 11 \cdot 4^4 + \dots + 23 \cdot 4^8 + 26 \cdot 262,144 = 1,922,392 + 26 \cdot 262,144 \quad :$$

$$2 \cdot 4 + 5 \cdot 4^2 + 8 \cdot 4^3 + 11 \cdot 4^4 + \dots + 23 \cdot 4^8 + 26 \cdot 262,144 = 8,738,136 \quad :$$

$$8,738,136 \quad :$$

$$a > 0, f(x) = \frac{x^2 - a}{x^2 + 3a} - 1 \tag{1}$$

x (x) $x^2 + 3a$ $a > 0$ -
 x :

(2)

$$f'(x) = \frac{2x(x^2 + 3a) - 2x(x^2 - a)}{(x^2 + 3a)^2}$$

$$f'(x) = \frac{2x(x^2 + 3a - x^2 + a)}{(x^2 + 3a)^2}$$

$$f'(x) = \frac{8ax}{(x^2 + 3a)^2}$$

$x < 0$ $x > 0$ $a > 0$ - , $x = 0$ $8ax$
 $x < 0$, $x > 0$ - :

(3)

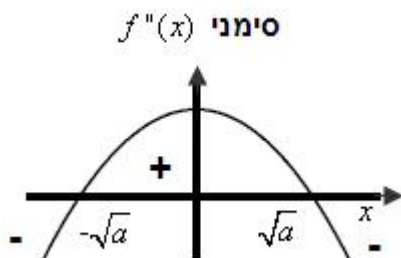
$$f''(x) = 8a \cdot \frac{(x^2 + 3a)^2 - 2x(x^2 + 3a) \cdot 2x}{(x^2 + 3a)^4}$$

$$f''(x) = 8a \cdot (x^2 + 3a) \cdot \frac{(x^2 + 3a - 4x^2)}{(x^2 + 3a)^4}$$

$$f''(x) = \frac{8a \cdot (x^2 + 3a)(3a - 3x^2)}{(x^2 + 3a)^4}$$

$$0 = 3a - 3x^2 \quad /:3$$

$$x = \pm\sqrt{a} \quad \leftarrow a > 0$$



, x $\frac{8a \cdot (x^2 + 3a)}{(x^2 + 3a)^4}$

$$x = -\sqrt{a}, x = \sqrt{a}$$

$$x = -\sqrt{a}, x = \sqrt{a} :$$

$x -$ (4)

$$f(x) = \frac{x^2 - a}{x^2 + 3a} - 1$$

$$0 = \frac{x^2 - a}{x^2 + 3a} - 1 \quad / \cdot (x^2 + 3a)$$

$$0 = x^2 - a - x^2 - 3a$$

$$a = 0$$

$a > 0 \quad x -$

$$f(0) = \frac{0^2 - a}{0^2 + 3a} - 1 = -1 \frac{1}{3} \quad y -$$

$(0, -1\frac{1}{3}) :$

(5)

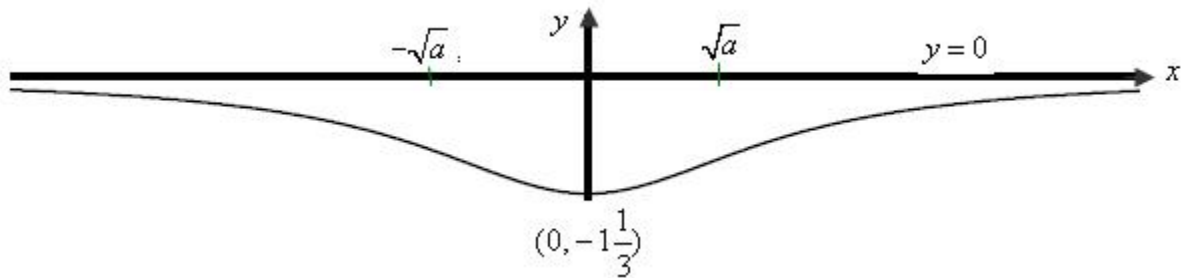
$$y - \quad y = 0 \quad , \quad \lim_{x \rightarrow \infty} \frac{x^2 - a}{x^2 + 3a} - 1 = \lim_{x \rightarrow \infty} \frac{1 - \frac{a}{x^2}}{1 + \frac{3a}{x^2}} - 1 = 1 - 1 = 0$$

$x -$

x

$y = 0 :$

$a > 0$



$$a < 0, \quad f(x) = \frac{x^2 - a}{x^2 + 3a} - 1 \quad (1)$$

$$x^2 + 3a \neq 0 \rightarrow x^2 \neq -3a \rightarrow x \neq \pm\sqrt{-3a} : \quad x^2 + 3a$$

$$x \neq \pm\sqrt{-3a} :$$

$$a < 0, \quad f''(x) = \frac{8a \cdot (x^2 + 3a)(3a - 3x^2)}{(x^2 + 3a)^4} \quad (2)$$

$$a < 0 \quad x \quad 3a - 3x^2 - , \quad (x^2 + 3a)$$

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$$g(x) = -\sqrt{x-4}, f(x) = \sqrt{-x-4}$$

$$-x-4 \geq 0 \rightarrow -x \geq 4 \rightarrow \boxed{x \leq -4} : f(x) = \sqrt{-x-4}$$

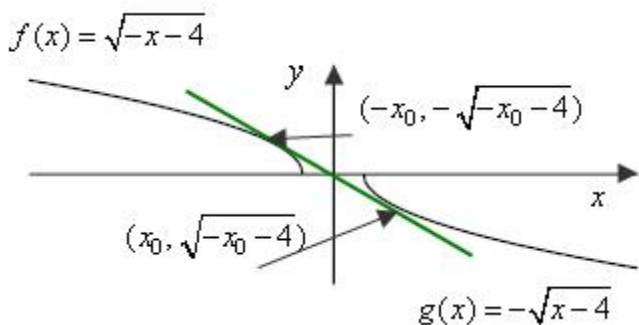
$$x-4 \geq 0 \rightarrow \boxed{x \geq 4} : g(x) = -\sqrt{x-4}$$

$$f'(x) = \frac{-1}{2\sqrt{-x-4}} \quad (1)$$

$$m = \frac{-1}{2\sqrt{-x_0-4}} \quad x = x_0$$

$$m = \frac{-1}{2\sqrt{-x_0-4}} \quad x =$$

$$g'(x) = \frac{-1}{2\sqrt{x-4}}$$



$$\begin{aligned} \frac{-1}{2\sqrt{x-4}} &= \frac{-1}{2\sqrt{-x_0-4}} \\ \sqrt{-x_0-4} &= \sqrt{x-4} \\ -x_0-4 &= x-4 \\ x &= -x_0 \end{aligned}$$

$$g(-x_0) = -\sqrt{-x_0-4} \rightarrow \boxed{(-x_0, -\sqrt{-x_0-4})}$$

$$(-x_0, -\sqrt{-x_0-4}) : g(x) = -\sqrt{x-4}$$

$$(x_0, \sqrt{-x_0-4}) : f(x) = \sqrt{-x-4}$$

(2)

$$\frac{-1}{2\sqrt{-x_0-4}} = \frac{-\sqrt{-x_0-4} - \sqrt{-x_0-4}}{-x_0 - x_0}$$

$$\frac{-1}{2\sqrt{-x_0-4}} = \frac{-2\sqrt{-x_0-4}}{-2x_0}$$

$$-x_0 = 2(-x_0-4)$$

$$-x_0 = -2x_0 - 8$$

$$x_0 = -8 \rightarrow g(8) = -\sqrt{8-4} = -2 \rightarrow \boxed{(8, -2)}$$

(8, -2) :

$$V = f \int_a^b f^2(x) dx$$

$$g(x) = -\sqrt{x-4}$$

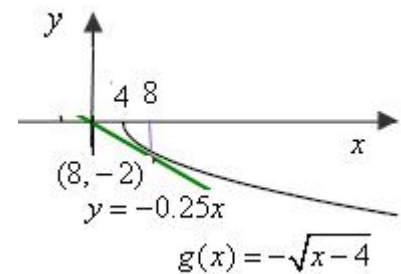
$$f(x) = \sqrt{-x-4}$$

$$m = \frac{-1}{2\sqrt{8-4}} = -0.25$$

$$(8, -2)$$

$$y + 2 = -0.25(x - 8)$$

$$y = -0.25x$$



*

) x -

- V_1

, x -

$$g(x) = -\sqrt{x-4}$$

- V_2

$$(4, 0)$$

$$V_2 = f \int_4^8 [(-\sqrt{x-4})^2] dx =$$

$$V_2 = f \int_4^8 [x-4] dx =$$

$$V_2 = f \left(\frac{x^2}{2} - 4x \right) \Big|_4^8$$

$$V_2 = f \left(\left(\frac{8^2}{2} - 4 \cdot 8 \right) - \left(\frac{4^2}{2} - 4 \cdot 4 \right) \right)$$

$$V_2 = 8f$$

$$V_1 = f \int_0^8 [(-0.25x)^2] dx =$$

$$V_1 = f \int_0^8 [0.0625x^2] dx =$$

$$V_1 = f \left(\frac{0.0625x^3}{3} \right) \Big|_0^8$$

$$V_1 = f \left(\left(\frac{0.0625 \cdot 8^3}{3} \right) - \left(\frac{0.0625 \cdot 0^3}{3} \right) \right)$$

$$V_1 = 10 \frac{2}{3} f$$

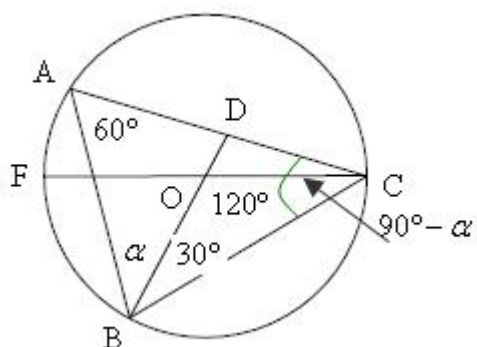
$$2 \cdot 2 \frac{2}{3} f = 5 \frac{1}{3} f$$

$$, \quad .V = V_1 - V_2 = 10 \frac{2}{3} f - 8f = 2 \frac{2}{3} f :$$

$$.5 \frac{1}{3} f$$

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() $\widehat{FB} = 180^\circ$ () CF
 $\angle BAC = 60^\circ$ $\widehat{BC} = \frac{2}{3} \cdot 180^\circ = 120^\circ$
 ()
 $\angle BAC = 60^\circ$:
 $\frac{S_{\triangle BAD}}{S_{\triangle BAC}}$.

.(, AC B - h) AC - AD

$$\frac{S_{\triangle BAD}}{S_{\triangle BAC}} = \frac{0.5AD \cdot h}{0.5AC \cdot h} = \frac{AD}{AC}$$

() $\angle BOC = 120^\circ$
 ($\triangle OBC$) $\angle OBC = \angle OCB = 30^\circ$
 ($180^\circ \triangle ABC$) $\angle DCB = 90^\circ - r$

$\triangle ABD$

$$\frac{AB}{\sin(180^\circ - (60^\circ + r))} = \frac{AD}{\sin r} \rightarrow AB = \frac{AD \sin(60^\circ + r)}{\sin r}$$

$\triangle ABC$

$$\frac{AC}{\sin(30^\circ + r)} = \frac{AB}{\sin(90^\circ - r)}$$

$$AC = \frac{AD \sin(60^\circ + r) \sin(30^\circ + r)}{\sin r \cos r} = \frac{2AD \sin(60^\circ + r) \sin(30^\circ + r)}{\sin 2r}$$

$$\frac{S_{\triangle BAD}}{S_{\triangle BAC}} = \frac{AD}{AC} = \frac{AD}{\frac{2AD \sin(60^\circ + r) \sin(30^\circ + r)}{\sin 2r}} = \frac{\sin 2r}{2 \sin(60^\circ + r) \sin(30^\circ + r)} :$$

$$\frac{S_{\triangle BAD}}{S_{\triangle BAC}} = \frac{\sin 2r}{2 \sin(60^\circ + r) \sin(30^\circ + r)} :$$

$$\frac{AD}{AB} = \frac{\sin r}{\sin(60^\circ + r)} : \quad \frac{AD}{AB} = \frac{2}{3} :$$

$$\frac{2}{3} = \frac{\sin r}{\sin(60^\circ + r)}$$

$$2(\sin 60^\circ \cos r + \cos 60^\circ \sin r) = 3 \sin r \quad /: \sin r \neq 0$$

$$\frac{\sqrt{3}}{\tan r} + 1 = 3 \quad \rightarrow \tan r = \frac{\sqrt{3}}{2}$$

$$\boxed{r = 40.89^\circ} \quad \leftarrow 0 < r < 90^\circ$$

$$r = 40.89^\circ :$$