

$$P = \dots$$

$$(P:1)$$

$$P = \dots$$

$$\left(\frac{0.25}{4} = \frac{1}{16}\right) \quad 16$$

$$\left(P = \frac{S_1/t_1}{S_2/t_2} \rightarrow P = \frac{S_1 \cdot t_2}{S_2 \cdot t_1} \rightarrow P = \frac{1}{P} \cdot 16 \rightarrow P^2 = 16\right) \quad \sqrt{16} = 4$$

. 4 :

. " 90 - B - A .

, $\frac{1}{5}$, 4:1

. " 72 - " 90:5=18 -

. " 18 - ,

" 30 , " 120 ,

. " 120 - " 72 - :

. " 30 - " 18 -

$$S_n = a_1 + a_2 + a_3 + \dots + a_n \quad \cdot a_n = n! \cdot n \quad , a_1, a_2, a_3, \dots, a_n \dots$$

$$: n = 1 \quad .1 .$$

$$S_1 = a_1 = 1! \cdot 1 = 1 < a_2 = 2! \cdot 2 = 4$$

$$n = 1 \quad ,$$

$$, (\quad) \quad n = k \quad .2$$

$$S_k < a_{k+1} :$$

$$" \quad , n = k + 1 \quad .3$$

$$S_{k+1} < a_{k+2}$$

$$\Leftrightarrow \frac{S_k}{\downarrow} + a_{k+1} < a_{k+2}$$

$$\Leftrightarrow a_{k+1} + a_{k+1} \leq a_{k+2}$$

$$, \quad , \quad - \quad ,$$

$$(\quad) \quad - \quad ,$$

$$\Leftrightarrow 2a_{k+1} \leq a_{k+2}$$

$$\Leftrightarrow 2(k+1)!(k+1) \leq (k+2)!(k+2)$$

$$\Leftrightarrow 2(k+1)!(k+1) \leq (k+1)!(k+2)(k+2)$$

$$k \quad 2 < k+2 \quad , \quad k+1 < k+2 \quad , \quad (k+1)! = (k+1)!$$

.

$$, n = 1 \quad .4$$

$$, n = k$$

$$n = k + 1$$

$$\cdot \quad n \quad , \quad - \quad ,$$

$$S_1 + S_2 + S_3 + \dots + S_{10} < S_{11} - a_1 \quad .$$

$$: \quad , S_1 + S_2 + S_3 + \dots + S_{10} < a_2 + a_3 + a_4 + \dots + a_{11} : \quad n = 1, 2, 3, \dots, 10 \quad ,$$

$$S_1 + S_2 + S_3 + \dots + S_{10} < a_1 + a_2 + a_3 + a_4 + \dots + a_{11} - a_1$$

$$S_1 + S_2 + S_3 + \dots + S_{10} < S_{11} - a_1$$

. :

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$$0 \leq x \leq \frac{2f}{3}$$

$$f(x) = \cos^3(3x - f) :$$

$$f(x) = \cos^3(3x - f) = \cos^3(f - 3x) = -\cos^3 3x$$

$$f(0) = -\cos^3(3 \cdot 0) = -1 \rightarrow (0, -1)$$

$$, x = 0 \quad y = -$$

$$, y = 0 \quad x =$$

$$0 = -\cos^3 3x \rightarrow \cos 3x = 0 \rightarrow 3x = \frac{f}{2} + f k \rightarrow x = \frac{f}{6} + \frac{f}{3} k$$

$$. x = \frac{f}{2} \quad k = 1 \quad , x = \frac{f}{6} \quad k = 0$$

$$. (\frac{f}{2}, 0) , (\frac{f}{6}, 0) , (0, -1) :$$

:

,

$$(0, -1), f(\frac{2f}{3}) = -\cos^3(3 \cdot \frac{2f}{3}) = -1 \rightarrow (\frac{2f}{3}, -1)$$

$$f'(x) = 3 \cos^2 3x \sin 3x$$

$$0 = 3 \cos^2 3x \sin 3x$$

$$\sin 3x = 0 \quad \cos 3x = 0 \rightarrow (\frac{f}{6}, 0), (\frac{f}{2}, 0) \text{ have been proved}$$

$$3x = f k \quad x = \frac{f}{3} k$$

$$k = 1 \rightarrow x = \frac{f}{3} \rightarrow f(\frac{f}{3}) = -\cos^3(3 \cdot \frac{f}{3}) = 1 \rightarrow (\frac{f}{3}, 1)$$

$$k = 0, 2 \rightarrow x = 0, x = \frac{2f}{3} \text{ end points}$$

,

,

$$(\frac{f}{6}, 0), (\frac{f}{2}, 0)$$

0		$\frac{f}{6}$		$\frac{f}{3}$		$\frac{f}{2}$		$\frac{2f}{3}$	x
-1		0		1		0		-1	f(x)
				0					f'(x)
Min	↖		↖	Max	↘		↘	Min	

$$. (\frac{f}{3}, 1) , (\frac{2f}{3}, -1) , (0, -1) :$$

"

(1).

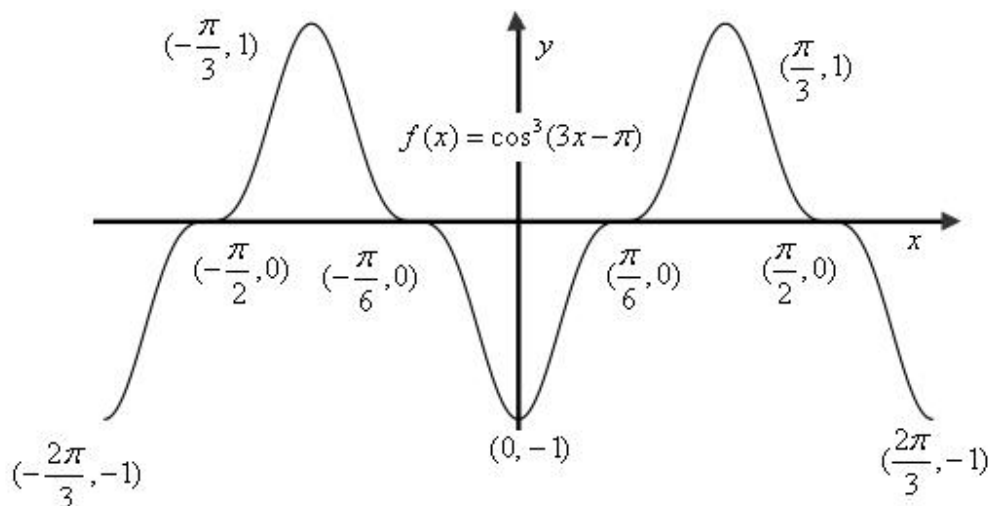
$$f(x) = -\cos^3 3x$$

$$f(-x) = -\cos^3(3(-x)) = -\cos^3(-3x) = -\cos^3 3x$$

$$f(-x) = f(x)$$

. y - (2)

. x - $(-\frac{f}{2}, 0), (-\frac{f}{6}, 0)$
 , $(-\frac{f}{3}, 1), (-\frac{2f}{3}, -1)$
 , $(0, -1)$
 :



. 0 , .

. y = -1 , (0, -1)

.(,)

. y = 1 $(-\frac{f}{3}, 1) - (\frac{f}{3}, 1)$

, 0 , $(-\frac{f}{2}, 0), (-\frac{f}{6}, 0), (\frac{f}{6}, 0), (\frac{f}{2}, 0)$

. y = 0

. y = 0 , y = 1 , y = -1 :

$$f(x) = \frac{bx+1}{\sqrt{x^2-a}}$$

$a=9$, $3^2 - a = 0$, $x=3$
 $b=1$, $1 = \frac{bx}{|x|}$, $x=3$
 $y=1$
 $b=1, a=9 :$

$$f(x) = \frac{x+1}{\sqrt{x^2-9}}$$

0 - , (1)

$x = -3, 3$, $x^2 - 9 > 0$

$x < -3$, $x > 3 :$

$x=0$, y (2)

$x = -1$, $y = 0$, x

$:$
 $:$ (3)

$$f(x) = \frac{x+1}{\sqrt{x^2-9}} = \frac{x+1}{|x|\sqrt{1-\frac{9}{x^2}}}$$

$$\lim_{x \rightarrow +\infty} \frac{x+1}{|x|\sqrt{1-\frac{9}{x^2}}} = \lim_{x \rightarrow +\infty} \frac{x+1}{x\sqrt{1-\frac{9}{x^2}}} = \frac{1}{1} \rightarrow \boxed{y=1}$$

$$\lim_{x \rightarrow -\infty} \frac{x+1}{|x|\sqrt{1-\frac{9}{x^2}}} = \lim_{x \rightarrow -\infty} \frac{x+1}{-x\sqrt{1-\frac{9}{x^2}}} = \frac{1}{-1} \rightarrow \boxed{y=-1}$$

$$\lim_{x \rightarrow 3^+} \frac{x+1}{\sqrt{x^2-9}} = \lim_{x \rightarrow 3^+} \frac{4}{0^+} = +\infty \rightarrow \boxed{x=3}$$

$$\lim_{x \rightarrow -3^-} \frac{x+1}{\sqrt{x^2-9}} = \lim_{x \rightarrow -3^-} \frac{-2}{0^+} = -\infty \rightarrow \boxed{x=-3}$$

$x = -3, x = 3 :$, $y = -1, y = 1 :$

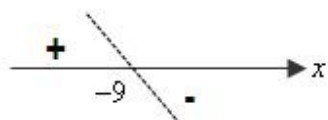
(4)

$$f(x) = \frac{x+1}{\sqrt{x^2-9}}$$

$$f'(x) = \frac{\sqrt{x^2-9} - \frac{2x(x+1)}{2\sqrt{x^2-9}}}{x^2-9}$$

$$f'(x) = \frac{x^2-9-x^2-x}{(x^2-9)\sqrt{x^2-9}}$$

$$f'(x) = \frac{-9-x}{(x^2-9)\sqrt{x^2-9}}$$

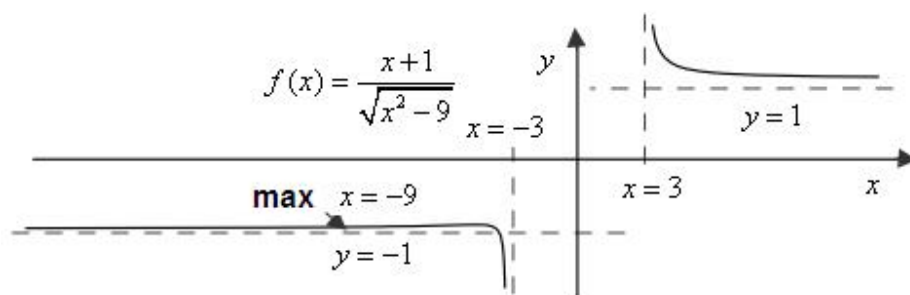


$x = -9$ 0 , ,

$x > 3$ $-9 < x < -3$ $x < -9$

$x < -9$: , $-9 < x < -3$ $x > 3$: :

$x < -3$ $x > 3$

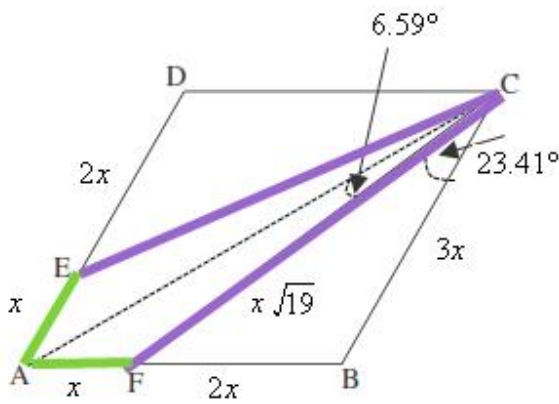


$$3 < k < t \quad , \int_k^t (f'(x)) dx$$

$$\int_k^t (f'(x)) dx = f(x) \Big|_k^t = f(t) - f(k)$$

$3 < k < t$ - $x > 3$,

$f(t) - f(k) < 0$ $f(t) < f(k)$ -



- () AE = AF = x
- () FB = 2AF = 2x
- 3x () AB = 3x
- () DE = 2x
- () ∠DCB = 60°
- (180° -) ∠FBC = 120°

ΔFCB

$$(CF)^2 = (FB)^2 + (BC)^2 - 2FB \cdot BC \cdot \cos \angle FBC$$

$$(CF)^2 = (2x)^2 + (3x)^2 - 2 \cdot 2x \cdot 3x \cdot \cos 120^\circ$$

$$(CF)^2 = 19x^2$$

$$\boxed{CF = x\sqrt{19}}$$

ΔFCB

$$\frac{FB}{\sin \angle FCB} = \frac{FC}{\sin \angle FBC} \rightarrow \frac{2x}{\sin \angle FCB} = \frac{x\sqrt{19}}{\sin 120^\circ}$$

$$\frac{2x \sin 120^\circ}{x\sqrt{19}} = \sin \angle FCB$$

$$\boxed{\angle FCB = 23.41^\circ}$$

∠FCB = 23.41° :

b AC

$$() \angle ACB = 30^\circ$$

$$() \angle ACF = 6.59^\circ$$

$$() \angle CAF = 30^\circ$$

$$(180^\circ \text{ } \Delta ACF \text{ }) \angle AFC = 143.41^\circ$$

ΔACF

$$\frac{FC}{\sin \angle CAF} = \frac{AC}{\sin \angle AFC} \rightarrow \frac{x\sqrt{19}}{\sin 30^\circ} = \frac{b}{\sin 143.41^\circ}$$

$$x\sqrt{19} = 0.8388b \rightarrow \boxed{FC = 0.8388b}$$

$$x = 0.1924b \rightarrow \boxed{AF = 0.1924b}$$

$$\text{AECF} \quad () \quad \Delta FCB \cong \Delta ECD$$

$$2 \cdot 0.8388b + 2 \cdot 0.1924b = 2.0624b : \text{AECF}$$

" 2.0624b AECF :